

# Supplemental: Visualizing the Uncertainty of Graph-based 2D Segmentation with Min-path Stability

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## 1. Pseudocode of Major Algorithms

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### Algorithm 1 Live-wire Min-path Stability

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**Input:** constraints:  $C$ ; trees:  $\mathcal{T}$ ; graph:  $\mathcal{G}$   
**Output:**  $\mathcal{S}$   
**for all** updated  $c_i \in C$  **do**  
    compute  $\mathcal{T}_i$   
**end for**  
**for all**  $p \in \mathcal{G}$  **do**  
     $\mathcal{S}(p) \leftarrow \infty$   
    **for all** pairs of consecutive  $c_i, c_j \in C$  **do**  
         $\mathcal{S}^{ij}(p) \leftarrow \text{cost}(p, \mathcal{T}_i) + \text{cost}(p, \mathcal{T}_j)$   
         $\mathcal{S}(p) \leftarrow \min(\mathcal{S}(p), \mathcal{S}^{ij}(p))$   
    **end for**  
**end for**

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### Algorithm 2 Graph Cut Smoothness Min-path Stability

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**Input:** annuli:  $F$ ; trees:  $\mathcal{T}$ ; graph:  $\mathcal{G}$   
**Output:**  $\mathcal{S}_s$   
**for all**  $f^i \in F$  **do**  
     $\mathcal{N}^i, \hat{\mathcal{N}}^i \leftarrow \text{splitAndReplicate}(f^i)$   
    **for all**  $n_j^i \in \mathcal{N}^i$  and  $\hat{n}_j^i \in \hat{\mathcal{N}}^i$  **do**  
        compute  $\mathcal{T}_j^i$  and  $\hat{\mathcal{T}}_j^i$   
    **end for**  
**end for**  
 $\mathcal{S}_s(p) \leftarrow \infty$   
**for all**  $p \in \mathcal{G}$  **do**  
    **for all**  $f^i \in F$  **do**  
         $\mathcal{S}_s^i(p) \leftarrow \infty$   
        **for all**  $n_j^i \in \mathcal{N}^i$  and  $\hat{n}_j^i \in \hat{\mathcal{N}}^i$  **do**  
             $\mathcal{S}_s^i(p) \leftarrow \min(\text{cost}(p, \mathcal{T}_j^i) + \text{cost}(p, \hat{\mathcal{T}}_j^i), \mathcal{S}_s^i(p))$   
        **end for**  
    **end for**  
     $\mathcal{S}_s(p) \leftarrow \min(\mathcal{S}_s^i(p), \mathcal{S}_s(p))$   
**end for**

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**Algorithm 3** Alternative Minimum Paths

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**Input:** queue:  $Q$ ; trees:  $\mathcal{T}$ ; graph:  $\mathcal{G}$   
**Output:** AP

**procedure** COUNT( $p, i$ )  
   $path = path(p, \mathcal{T}_i)$   
   $v, \omega \leftarrow 0$   
  **for all**  $n \in path$  **do**  $\triangleright p$  to root  
    **if**  $V_i(n)$  **then**  
       $(v, \omega) \leftarrow (v, \omega) + B_i(n)$   
      **return**  $(v, \omega, path, n)$   
    **end if**  
    **if**  $n \in AP$  **then**  $\omega \leftarrow \omega + 1$  **else**  $v \leftarrow v + 1$  **end if**  
  **end for**  
  **return**  $(v, \omega, path, n)$   
**end procedure**

**procedure** REJECT( $path, n, i$ )  
   $(v, \omega) = B_i(n)$   
  **for all**  $m \in path$  **do**  $\triangleright n$  to  $p$ , skip  $n$  unless  $n$  is root  
    **if**  $n \in AP$  **then**  $\omega \leftarrow \omega + 1$  **else**  $v \leftarrow v + 1$  **end if**  
     $B_i(m) = (v, \omega), V_i(m) = \text{True}$   
  **end for**  
**end procedure**

**procedure** FIND  
  Reset all  $V_i, V_j, B_i$ , and  $B_j$   
  **for all**  $p \in \mathcal{G}$  **do**  $\triangleright$  by ascending cost from  $Q$   
     $(v_i, \omega_i, path_i, n_i) \leftarrow \text{COUNT}(p, i)$   
     $(v_j, \omega_j, path_j, n_j) \leftarrow \text{COUNT}(p, j)$   
    **if**  $(\omega_i + \omega_j) / (v_i + v_j + \omega_i + \omega_j) \leq \beta$  **then**  
       $AP = AP + (path_i \cup path_j)$   
      **if**  $|AP| == k$  **then return**  $AP$  **else** FIND **end if**  
    **else**  
      REJECT( $path_i, n_i, i$ ), REJECT( $path_j, n_j, j$ )  
    **end if**  
  **end for**  
**end procedure**

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